Cryptography

Lecture 12

Announcements

- Midterm Next Class on Wednesday 3/13
- Study Materials
  - Review sheet posted on course webpage, solutions posted on Canvas
  - Cheat Sheet posted on Canvas
  - Extra practice folder on Canvas with last year's HW5 and solutions as well as an additional class exercise and solutions

Agenda

- Last time:
  - Domain Extension for MACs (K/L 4.4) and Class Exercise solutions
  - CCA security (K/L 3.7)
  - Unforgeability for Encryption (K/L 4.5)
- This time:
  - Authenticated Encryption (K/L 4.5)
  - Review for Midterm

Chosen Ciphertext Security

CCA Security

The CCA Indistinguishability Experiment $PrivK^{cca}{}_{A,\Pi}(n)$:

1. A key k is generated by running $Gen(1^n)$.
2. The adversary A is given input 1^n and oracle access to $Enc_k(\cdot)$ and $Dec_k(\cdot)$, and outputs a pair of messages m_0, m_1 of the same length.
3. A random bit $b \leftarrow \{0,1\}$ is chosen, and then a challenge ciphertext $c \leftarrow Enc_k(m_b)$ is computed and given to A.
4. The adversary A continues to have oracle access to $Enc_k(\cdot)$ and $Dec_k(\cdot)$, but is not allowed to query the latter on the challenge ciphertext itself. Eventually, A outputs a bit b'.
5. The output of the experiment is defined to be 1 if $b' = b$, and 0 otherwise.

CCA Security

A private-key encryption scheme $\Pi = (Gen, Enc, Dec)$ has indistinguishable encryptions under a chosen-ciphertext attack if for all ppt adversaries A there exists a negligible function $negl$ such that

$$\Pr\left[PrivK^{cca}{}_{A,\Pi}(n) = 1\right] \leq \frac{1}{2} + negl(n),$$

where the probability is taken over the random coins used by A, as well as the random coins used in the experiment.

Authenticated Encryption

The unforgeable encryption experiment $EncForge_{A,\Pi}(n)$:

1. Run $Gen(1^n)$ to obtain key k.
2. The adversary A is given input 1^n and access to an encryption oracle $Enc_k(\cdot)$. The adversary outputs a ciphertext c.
3. Let $m \coloneqq Dec_k(c)$, and let Q denote the set of all queries that A asked its encryption oracle. The output of the experiment is 1 if and only if (1) $m \neq \perp$ and (2) $m \notin Q$.

Authenticated Encryption

Definition: A private-key encryption scheme Π is unforgeable if for all ppt adversaries A, there is a negligible funcion neg such that:

$$\Pr\left[EncForge_{A,\Pi}(n) = 1\right] \leq neg(n)\,.$$

Definition: A private-key encryption scheme is an authenticated encryption scheme if it is CCA-secure and unforgeable.

Generic Constructions

Encrypt-and-authenticate

Encryption and message authentication are computed independently in parallel.

$$c \leftarrow Enc_{k_E}(m) \qquad t \leftarrow Mac_{k_M}(m)$$

$$\langle c, t \rangle$$

Is this secure? NO!

Authenticate-then-encrypt

Here a MAC tag t is first computed, and then the message and tag are encrypted together.

$$t \leftarrow Mac_{k_M}(m) \qquad c \leftarrow Enc_{k_E}(m||t)$$

c is sent

Is this secure? NO! Encryption scheme may not be CCA-secure.

Encrypt-then-authenticate

The message m is first encrypted and then a MAC tag is computed over the result

$$c \leftarrow Enc_{k_E}(m) \quad t \leftarrow Mac_{k_M}(c)$$

$$\langle c, t \rangle$$

Is this secure? YES! As long as the MAC is strongly secure.