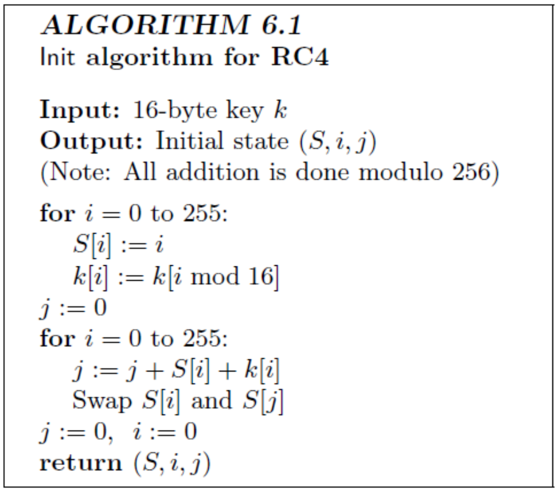
ENEE/CMSC/MATH 456: Cryptography
Stream Cipher Class Exercise 4/1/19



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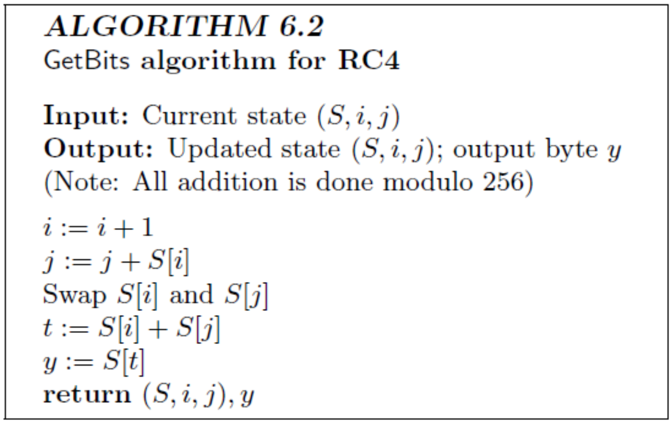
ALGORITHM 6.1
Init algorithm for RC4

Input: 16-byte key $k$
Output: Initial state $(S, i, j)$
(Note: All addition is done modulo 256)

for $i = 0$ to 255:
    $S[i] := i$
    $k[i] := k[i \bmod 16]$
$j := 0$
for $i = 0$ to 255:
    $j := j + S[i] + k[i]$
    Swap $S[i]$ and $S[j]$
$j := 0,\ \ i := 0$
return $(S, i, j)$
```



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ALGORITHM 6.2
GetBits algorithm for RC4

Input: Current state $(S, i, j)$
Output: Updated state $(S, i, j)$; output byte $y$
(Note: All addition is done modulo 256)

$i := i + 1$
$j := j + S[i]$
Swap $S[i]$ and $S[j]$
$t := S[i] + S[j]$
$y := S[t]$
return $(S, i, j), y$
```

Let S^0 denote the initial state, S^i denote the state after i calls to **GetBits**.

Consider Event 1: $(S^0[2] = 0) \wedge (S^0[1] = X \neq 2)$

What is the probability that Event 1 occurs? (For this part, assume Init outputs a perfectly random permutation of the values from 0 to 255) ______________________________

Assuming Event 1 occurs, what is the value of $S^1[X]$ (i.e. the value in position $S[X]$ after the first iteration? _____________

Assuming Event 1 occurs, what is the value of $S^2[X], S^2[2]$ (i.e. the values in positions $S[X]$ and $S[2]$ after the second iteration? _______________________________

Assuming Event 1 occurs, what value (call this V) is outputted in the second iteration?

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Assuming Event 1 does not occur, V is uniformly distributed.

Towards what value is V biased and with what probability? ______________________