Introduction to Cryptology ENEE459E/CMSC498R: Homework 12

Due by 2pm on 5/14/2015.

- Consider the following variant of El Gamal encryption. The private key is (G, g, q, x) and the public key is G, g, q, h), where h = g^x and x ∈ Z_q is chosen uniformly. To encrypt a message m ∈ M, in the message space M, choose a uniform r ∈ Z_q, compute c₁ := g^rmodp and c₂ := h^r ⋅ g^m, and let the ciphertext be (c₁, c₂). For which message spaces M will the above scheme be a good encryption scheme?
- 2. Consider the following variant of El Gamal encryption. Let p = 2q + 1, let G be the group of squares modulo p, and let g be a generator of G. The private key is (G, g, q, x) and the public key is G, g, q, h), where h = g^x and x ∈ Z_q is chosen uniformly. To encrypt a message m ∈ Z_q, choose a uniform r ∈ Z_q, compute c₁ := g^rmodp and c₂ := h^r + mmodp, and let the ciphertext be ⟨c₁, c₂⟩. Is this scheme CPA-secure? Prove your answer.
- 3. Consider the following modified version of padded RSA encryption: Assume messages to be encrypted have length exactly ||N||/2. To encrypt, first compute *m̂* := 0x00||r||0x00||m where r is a uniform string of length ||N||/2 − 16. Then compute the ciphertext c := [*m̂*^emodN]. When decrypting a ciphertext c, the receiver computes *m̂* := [c^dmodN] and returns an error of *m̂* does not consist of 0x00 followed by ||N||/2 − 16 arbitrary bits followed by 0x00. Show that this scheme is not CCA-secure. Why is it easier to construct a chosen-ciphertext attack on this scheme than on PKCS 1 v1.5?
- 4. In Section 12.4.1 we showed an attack on the plain RSA signature scheme in which an attacker forges a signature on an arbitrary message using two signing queries. Show how an attacker can forge a signature on an arbitrary message using a single signing query.